

If we have N players, how many coalitions are there?

Let's examine 2 players named A and B. I'll write my coalitions with braces (curly brackets) to make seeing them easier. And it happens to be proper mathematical form as well.

There's a coalition with both of them. Then two coalitions with one person. Also we'll throw in the coalition with nobody, the empty coalition.

2 players { }, {A}, {B}, {AB}.

Now for 3 players we could organize it by thinking of how many people are in the coalition. So write out the zero player coalition, all 3 one player coalitions, the two player coalitions, and the three player coalition. But there's a sneaky way of doing it.

3 players--A, B, and C. Can I list off all the coalitions that don't have C? Yep, did it above. So I'll copy and paste.

{ }, {A}, {B}, {AB}. All the remaining coalitions have C as a member. And we can copy and paste again, and just add C.

{ }, {A}, {B}, {AB} and then { C}, {AC}, {BC}, {ABC}.

I can use this same trick again for 4 players.

{ }, {A}, {B}, {AB}, {C}, {AC}, {BC}, {ABC} from above and {D}, {AD}, {BD}, {ABD}, {CD}, {ACD}, {BCD}, {ABCD}.

Each player added doubles the number of coalitions.

Number of Players || Number of coalitions

0	1. Yeah, if you have 0 players there is one coalition, the empty coalition!
1	2 { }, {A}
2	4 { }, {A}, {B}, {AB}
3	8 { }, {A}, {B}, {AB}, {C}, {AC}, {BC}, {ABC}

And so on. We can write this a better way.

Number of Players || Number of coalitions

0	1 = 2 <sup>0</sup>
1	2 = 2 <sup>1</sup>
2	4 = 2 <sup>2</sup>
3	8 = 2 <sup>3</sup>
4	16 = 2 <sup>4</sup>
5	32 = 2 <sup>5</sup>
Skip to a general number. . .	
N	2 <sup>N</sup>

So, to answer the question, if you have N players there are 2<sup>N</sup> coalitions if you count the empty coalition or 2<sup>N</sup> - 1 if you don't.